

QUESTION PAPER WITH SOLUTION

MATHEMATICS _ 4 Sep. _ SHIFT - 2











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ANSWER KEY

हमारा विश्वास... हर एक विद्यार्थी है खास

Suppose the vectors x_1 , x_2 and x_3 are the solutions of the system of linear equations, Ax=b when the vector b on the right side is equal to b_1 , b_2 and b_3 respectively. if **Q.1**

$$x_1 = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}, x_2 = \begin{bmatrix} 0 \\ 2 \\ 1 \end{bmatrix}, x_3 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, b_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, b_2 = \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix} \text{ and } b_3 = \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix}, \text{ then the determinant of A is equal to } b_1 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, b_2 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

- (1)2
- (2) $\frac{1}{2}$ (3) $\frac{3}{2}$
- (4) 4

Sol. (1)

$$A = \begin{bmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & a_9 \end{bmatrix}_{3\times 3}$$

$$a_1 + a_2 + a_3 = 1$$
 $2a_2 + a_3 = 0$

$$a_4 + a_5 + a_6 = 0$$
 $2a_5 + a_6 = 2$

$$a_7 + a_8 + a_9 = 0$$
 $2a_8 + a_9 = 0$

$$a_3 = 0, a_6 = 0, a_9 = 2$$

$$\therefore a_8 = -1, a_5 = 1, \quad a_2 = 0 \implies a_1 = \phi, a_4 = -1, \quad a_7 = -1$$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ -1 & -1 & 2 \end{bmatrix}$$

$$|A| = 2(1) = 2$$

If a and b are real numbers such that $(2+\alpha)^4=a+b\alpha$, where $\alpha=\frac{-1+i\sqrt{3}}{2}$ then a+b is **Q.2**

equal to:

- (1)33
- (2)57
- (3)9
- (4)24

Sol.

$$(2+\alpha)^4 = a + b\alpha$$

$$\left(2 + \frac{\sqrt{3}i - 1}{2}\right)^4 = a + b\alpha$$

$$\left(\frac{3+\sqrt{3}i}{2}\right)^4 = 9\left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^4$$

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$$9\left\{e^{i\pi/6}\right\}^4 = 9e^{i2\pi/3} = 9\left(\frac{-1}{2} + \frac{\sqrt{3}i}{2}\right) = \frac{-9}{2} + \frac{9\sqrt{3}}{2}i$$

$$-\frac{9}{2} + \frac{9\sqrt{3}}{2}i = a + b\left(\frac{-1}{2} + \frac{i\sqrt{3}}{2}\right)$$

$$=a-\frac{b}{2}+\frac{bi\sqrt{3}}{2}$$

$$\therefore \frac{b\sqrt{3}}{2} = \frac{9\sqrt{3}}{2} \Rightarrow b = 9$$

$$a = 0 : a + b = 9$$

Q.3 The distance of the point (1, -2, 3) from the plane x-y+z=5 measured parallel to the line $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$

(1)
$$\frac{1}{7}$$

(3)
$$\frac{7}{5}$$

Sol. (4

Equation of line through (1,-2,3) whose dr's are (2,3,-6)

$$\frac{x-1}{2} = \frac{y+2}{3} = \frac{z-3}{-6} = \lambda$$

any point on line $(2\lambda + 1, 3\lambda - 2, -6\lambda + 3)$

put in
$$(x - y + z = 5)$$

$$2\lambda + 1 - 3\lambda + 2 - 6\lambda + 3 = 5$$

$$-7\lambda = -1$$

$$\lambda = \frac{1}{7}$$

distance =
$$\sqrt{(2\lambda)^2 + (3\lambda)^2 + (6\lambda)^2}$$

$$\sqrt{4\lambda^2 + 9\lambda^2 + 36\lambda^2} = 7\lambda = 1$$

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Let $f:(0,\infty)\to(0,\infty)$ be a differentiable function such that f(1)=e and $\lim_{t\to x}\frac{t^2f^2(x)-x^2f^2(t)}{t-x}=0$. **Q.4**

If f(x)=1, then x is equal to:

- (1)e
- (2) 2e
- (3) $\frac{1}{e}$
- (4) $\frac{1}{2e}$

Sol. (3)

$$f(1) = e$$

$$\lim_{t \to x} \frac{t^2 f^2(x) - x^2 f^2(t)}{t - x}$$

L' Hospital

$$\lim_{t \to x} \left(2tf^{2}(x) - 2x^{2}f(t) \cdot f'(t) \right)$$

$$\Rightarrow 2xf^2(x) - 2x^2f(x) \cdot f'(x) = 0$$

$$2xf(x)\big\{f(x)-xf'(x)\big\}=0$$

$$=) \quad \frac{f'(x)}{f(x)} = \frac{1}{x}$$

$$\ln f(x) = \ln x + \ln c$$

$$f(x) = cx$$

if
$$x = 1$$
, $e = c$

$$y = ex$$

$$\therefore \text{ if } f(x) = 1 \implies x = \frac{1}{e}$$

Q.5 Contrapositive of the statement:

'If a function f is differentiable at a, then it is also continuous at a', is:

- (1) If a function f is not continuous at a, then it is not differentiable at a.
- (2) If a function f is continuous at a, then it is differentiable at a.
- (3) If a function f is continuous at a, then it is not differentiable at a.
- (4) If a function f is not continuous at a, then it is differentiable at a.
- Sol. (1)

Contrapositive of $P \rightarrow q = \sim q \rightarrow \sim p$

- The minimum value of $2^{sinx} + 2^{cosx}$ is: **Q.6**
 - (1) $2^{1-\sqrt{2}}$
- (2) $2^{1-\frac{1}{\sqrt{2}}}$
- (3) $2^{-1+\sqrt{2}}$
- (4) $2^{-1+\frac{1}{\sqrt{2}}}$

Sol.

$$y = 2^{\sin x} + 2^{\cos x}$$

by $Am \ge GM$

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$$\frac{2^{sin\,x} + 2^{cos\,x}}{2} \geq \sqrt{2^{sin\,x + cos\,x}}$$

$$2^{sinx} + 2^{cosx} \ge 2^{1.2} \frac{sin x + cos x}{2}$$

$$2^{\text{sinx}} + 2^{\text{cosx}} \geq 2^{\frac{2 + \sin x + \cos x}{2}} \ \ \therefore \ \left(2^{\text{Sinx}} + 2^{\text{cosx}}\right)_{\text{min}} = \ 2^{\frac{2 - \sqrt{2}}{2}} = \ 2^{\frac{-1}{\sqrt{2}} + 1}$$

Q.7 If the perpendicular bisector of the line segment joining the points P(1,4) and Q(k, 3) has y-intercept equal to -4, then a value of k is:

$$(1) - 2$$

(2)
$$\sqrt{15}$$

(3)
$$\sqrt{14}$$

$$(4) - 4$$

Sol. (4

$$m_{PQ} = \frac{4-3}{1-k} \Longrightarrow m_{\perp} = k-1$$

mid point of
$$PQ = \left(\frac{k+1}{2}, \frac{7}{2}\right)$$

equation of perpendicular bisector

$$y - \frac{7}{2} = (k-1)\left(x - \frac{k+1}{2}\right)$$

for y intercept put x = 0

$$y = \frac{7}{2} - \left(\frac{k^2 - 1}{2}\right) = -4$$

$$\frac{k^2 - 1}{2} = \frac{15}{2} \implies k = \pm 4$$

Q.8 The area (in sq. units) of the largest rectangle ABCD whose vertices A and B lie on the x-axis and vertices C and D lie on the parabola, $y=x^2-1$ below the x-axis, is:

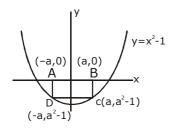
(1)
$$\frac{2}{3\sqrt{3}}$$

(2)
$$\frac{4}{3}$$

(3)
$$\frac{1}{3\sqrt{3}}$$

(4)
$$\frac{4}{3\sqrt{3}}$$

Sol. (4



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Area =
$$2a(a^2-1)$$

 $A = 2a^3 - 2a$

$$\frac{dA}{da} = 6a^2 - 2 = 0$$

$$a = \pm 1\sqrt{3}$$

$$A_{\text{max}} = \frac{-2}{3\sqrt{3}} + \frac{2}{\sqrt{3}} = \frac{-2+6}{3\sqrt{3}} = \frac{4}{3\sqrt{3}}$$

- The integral $\int_{\pi/6}^{\pi/3} \tan^3 x \cdot \sin^2 3x (2 \sec^2 x \cdot \sin^2 3x + 3 \tan x \cdot \sin 6x) dx$ is equal to: 0.9

 - (1) $\frac{9}{2}$ (2) $-\frac{1}{18}$ (3) $-\frac{1}{9}$
- (4) $\frac{7}{18}$

Sol.

$$I = \int_{\pi/6}^{\pi/3} 2 \cdot \tan^3 x \sec^2 x \sin^4 3x + 3\tan^4 x \sin^2 3x. \ 2\sin 3x \cos 3x \ dx$$

$$= \frac{1}{2} \int_{\pi/6}^{\pi/3} 4 \tan^3 x \sec^2 x \sin^4 3x + 3.4 \tan^4 x \sin^3 3x \cos 3x dx$$

$$= \frac{1}{2} \int_{\pi/6}^{\pi/3} \frac{d}{dx} \left(\tan^4 x \sin^4 3x \right) dx$$

$$= \frac{1}{2} \left[\tan^4 x \sin^4 3x \right]_{\pi/6}^{\pi/3}$$

$$=\frac{1}{2}\left[9.(0)-\frac{1}{3}.\frac{1}{3}(1)\right]=-\frac{1}{18}$$

Q.10 If the system of equations

x+y+z=2

2x+4y-z=6

 $3x+2y+\lambda z=\mu$

has infinitely many solutions, then

(1)
$$\lambda - 2\mu = -3$$

(2)
$$2\lambda + \mu = 14$$

(1)
$$\lambda - 2\mu = -5$$
 (2) $2\lambda + \mu = 14$ (3) $\lambda + 2\mu = 14$ (4) $2\lambda - \mu = 5$

(4)
$$2\lambda - \mu = 5$$

Sol. (2)

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$$D = 0 \quad \begin{vmatrix} 1 & 1 & 1 \\ 2 & 4 & -1 \\ 3 & 2 & \lambda \end{vmatrix} = 0$$

$$(4\lambda + 2) - 1(2\lambda + 3) + 1(4 - 12) = 0$$

$$4\lambda + 2 - 2\lambda - 3 - 8 = 0$$

$$2\lambda = 9 \Longrightarrow \lambda = \frac{9}{2}$$

$$D_x = \begin{vmatrix} 2 & 1 & 1 \\ 6 & 4 & -1 \\ \mu & 2 & -9/2 \end{vmatrix} = 0$$

$$\Rightarrow \mu = 5$$

Now check option

$$2\lambda + \mu = 14$$

Q.11 In a game two players A and B take turns in throwing a pair of fair dice starting with player A and total of scores on the two dice, in each throw is noted. A wins the game if he throws total a of 6 before B throws a total of 7 and B wins the game if he throws a total of 7 before A throws a total of six. The game stops as soon as either of the players wins. The probability of A winning the game is:

(1)
$$\frac{5}{31}$$

(2)
$$\frac{31}{61}$$

(3)
$$\frac{30}{61}$$

(4)
$$\frac{5}{6}$$

sum total 7 = (1,6)(2,5)(3,4)(4,3)(5,2)(6,1)

$$P(sum) = \frac{6}{36}$$

sum total $6 \Rightarrow (1,5)(2,4)(3,3)(4,2)(5,1)$

P(sum 6) =
$$\frac{5}{36}$$

$$P(A_{win}) = P(6) + P(\overline{6}).P(\overline{7}).P(6) +$$

$$= \frac{5}{36} + \frac{31}{36} \times \frac{30}{36} \times \frac{5}{36} + \dots$$

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$$= \frac{\frac{5}{36}}{1 - \frac{31 \times 30}{36 \times 36}} \Rightarrow \frac{5 \times 36}{36 \times 36 - 31 \times 30} \Rightarrow \frac{5 \times 36}{1296 - 930} = \frac{5 \times 36}{366} \Rightarrow \frac{30}{61}$$

Q.12 If for some positive integer n, the coefficients of three consecutive terms in the binomial expansion of $(1+x)^{n+5}$ are in the ratio 5:10:14, then the largest coefficient in this expansion is :

(3) 462

Sol.

$$T_r: T_{r+1}: T_{r+2}$$

$${}^{n+5}C_{r-1}: {}^{n+5}C_r: {}^{n+5}C_{r+1} = 5:10:14$$

$$\frac{(n+5)!}{(r-1)! - (n+6-r)!}: \frac{(n+5)!}{r!(n+5-r)!} = \frac{5}{10}$$

$$\frac{r}{n+6-r} = \frac{1}{2}$$

$$\frac{r}{n+6-r} = \frac{1}{2} \qquad \frac{(r+1)!(n+4-r)!}{r!(n+5-r)!} = \frac{5}{7}$$

$$2r = n + 6 - r$$

$$3r = n + 6$$
 ...(1)
$$\frac{r+1}{n+5-r} = \frac{5}{7}$$
 $7r+7 = 5n + 25-5r$
 $12r = 5n + 18$...(2)

 $\therefore 4(n+6) = 5n + 18$ n = 6

∴ (1 + x) largest coeff = 11C₅ = 462

Q.13 The function
$$f(x) = \begin{cases} \frac{\pi}{4} + \tan^{-1} x, & |x| \le 1 \\ \frac{1}{2}(|x|-1), & |x| > 1 \end{cases}$$
 is :

- (1) both continuous and differentiable on $R-\{-1\}$
- (2) continuous on $R-\{-1\}$ and differentiable on $R-\{-1,1\}$
- (3) continuous on $R-\{1\}$ and differentiable on $R-\{-1,1\}$
- (4) both continuous and differentiable on R-{1}
- Sol. (3)

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$$f(x) = \begin{cases} \frac{\pi}{4} + \tan^{-1} x & x \in [-1, 1] \\ \frac{1}{2}(x-1) & x > 1 \\ \frac{1}{2}(-x-1) & x < -1 \end{cases}$$

at x = 1

$$f(1) = \frac{\pi}{2} f(1^+) = 0$$

$$f(1^+) = 0$$

 \therefore discontinuous \Rightarrow non diff. at x = - 1

$$f(-1)=0$$

$$f(-1) = 0$$
 $f(-1^-) = \frac{1}{2}\{+1-1\} = 0$

cont. at x = -1

$$f'(x) = \begin{cases} \frac{1}{1+x^2} & x \in [-1,1] \\ \frac{1}{2} & x > 1 \\ -\frac{1}{2} & x < -1 \end{cases}$$

Q.14 The solution of the differential equation $\frac{dy}{dx} - \frac{y + 3x}{\log_2(y + 3x)} + 3 = 0$ is: (where c is a constant of integration)

(1)
$$x - \log_{2}(y + 3x) = C$$

(2)
$$x - \frac{1}{2} (\log_e(y + 3x))^2 = C$$

(3)
$$x-2\log_{2}(y+3x)=C$$

(4)
$$y + 3x - \frac{1}{2} (\log_e x)^2 = C$$

Sol.

$$\frac{dy}{dx} - \frac{y+3x}{\ln(y+3x)} + 3 = 0$$

Let
$$ln(y + 3x) = t$$

$$\frac{1}{v+3x} \cdot \left(\frac{dy}{dx} + 3\right) = \frac{dt}{dx}$$

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$$\Rightarrow \left(\frac{dy}{dx} + 3\right) = \frac{y + 3x}{\ell n(y + 3x)}$$

$$\therefore (y+3x)\frac{dt}{dx} = \frac{y+3x}{t}$$

$$\Rightarrow$$
 tdt = dx

$$\frac{t^2}{2} = x + c$$

$$\frac{1}{2} \left(\ln \left(y + 3x \right) \right)^2 = x + c$$

Q.15 Let $\lambda \neq 0$ be in R. If α and β are the roots of the equation, $x^2 + x + 2\lambda = 0$ and α and γ are the roots of the equation, $\,_{3x^{^{2}}-10x\,+\,27\lambda\,=\,0}$, then $\,\frac{\beta\gamma}{\lambda}\,$ is equal to:

(3)18

Sol.

(3)
$$x^2 - x + 2\lambda = 0 (\alpha, \beta)$$

$$x^2 - x + 2\lambda = 0 (\alpha, \beta)$$

$$3x^2 - 10x + 27\lambda = 0(\alpha, \gamma)$$

$$3x^2 - 3x + 6\lambda = 0$$

$$\frac{-}{-7x+21\lambda} = 0$$

$$\therefore \alpha = 3\lambda$$
$$9\lambda^2 - 3\lambda + 2\lambda = 0$$

Put in equation

(2)9

$$9\lambda^2 - \lambda = 0 \implies \lambda = \frac{1}{9} \implies \alpha = \frac{1}{3}$$

$$\alpha.\beta = \frac{2}{9} \Rightarrow \beta = \frac{2}{3}$$

$$\alpha. \gamma = 1 \Rightarrow \gamma = 3$$

$$\therefore \frac{\beta r}{\lambda} \Rightarrow \frac{\frac{2}{3}.3}{\frac{1}{9}} = 18$$

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(4)36

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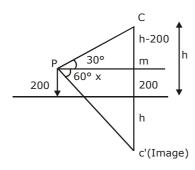
MOTION

Q.16 The angle of elevation of a cloud C from a point P, 200 m above a still lake is 30°. If the angle of depression of the image of C in the lake from the point P is 60°, then PC (in m) is equal to :

(1)
$$200\sqrt{3}$$

(2)
$$400\sqrt{3}$$

Sol. (3)



$$\frac{h-200}{r} = \tan 30^{\circ}$$

$$\frac{h+200}{x} = \tan 60^{\circ}$$

(2)30

$$\frac{h + 200}{h - 200} = 3$$

$$h + 200 = 3h - 600$$

$$2h = 800$$

$$h = 400$$

$$\therefore \frac{h-200}{PC} = \sin 30^{\circ}$$

$$PC = 400 \text{ m}$$

Q.17 Let $\bigcup_{i=1}^{50} X_i = \bigcup_{i=1}^{n} Y_i = T$, where each X_i contains 10 elements and each Y_i contains 5 elements. If each element of the set T is an element of exactly 20 of sets X, 's and exactly 6 of sets Y, 's, then n is equal to:

(3)50

(1)15

Sol.

$$\frac{50\times10}{20} = \frac{n\times5}{6}$$

$$\frac{50}{2} \times \frac{6}{5} = n \implies n = 30$$

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(4)45

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Q.18 Let x=4 be a directrix to an ellipse whose centre is at the origin and its eccentricity is $\frac{1}{2}$. If

 $P(1,\beta),\beta > 0$ is a point on this ellipse, then the equation of the normal to it at P is:

$$(1) 8x-2y=5$$

$$(2) 4x-2y=1$$

$$(3) 7x-4y=1$$

$$(4) 4x-3y=2$$

$$e = \frac{1}{2}$$

$$x = \frac{a}{e} = 4$$

$$\Rightarrow$$
 a = 2

$$e^2 = 1 - \frac{b^2}{a^2} \Rightarrow \frac{1}{4} = 1 - \frac{b^2}{4}$$

$$\frac{b^2}{4} = \frac{3}{4} \Rightarrow b^2 = 3$$

$$\therefore Ellipse \frac{x^2}{4} + \frac{y^2}{3} = 1$$

$$x = 1 ; \frac{1}{4} + \frac{\beta^2}{3} = 1$$

$$\frac{\beta^2}{3} = \frac{3}{4} \Rightarrow \beta = \frac{3}{2}$$

$$\Rightarrow P\left(1,\frac{3}{2}\right)$$

Equation of normal
$$\frac{a^2x}{x_1} - \frac{b^2y}{y_1} = a^2 - b^2$$

$$\frac{4x}{1} - \frac{3y}{\frac{3}{2}} = 4 - 3$$

$$4x - 2y = 1$$

- **Q.19** Let a_1 , a_2 , ..., a_n be a given A.P. whose common difference is an integer and $S_n = a_1 + a_2 + + a_n$. If $a_1 = 1$, $a_n = 300$ and $15 \le n \le 50$, then the ordered pair (S_{n-4}, a_{n-4}) is equal to:
- (1) (2480,248)
- (2) (2480,249)
- (3) (2490,249)
- (4) (2490,248)

Sol. 2

$$a_1 = 1$$
, $a_n = 300$, $15 \le n \le 50$
 $300 = 1 + (n - 1)d$

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Motion

$$(n-1) = \frac{299}{d}$$
d can 23 or 13
if n - 1 = 13
n = 14
reject
or d = 13
n - 1 = 23
n = 24
$$S_{20} = \frac{20}{2} \{2+19.13\}$$

$$a_{20} = 1 + 19.13$$

$$a_{20} = 248$$

$$a_{20} = 248$$

Q.20 The circle passing through the intersection of the circles, $x^2+y^2-6x=0$ and $x^2+y^2-4y=0$, having its centre on the line, 2x-3y+12=0, also passes through the point:

$$(2)(1,-3)$$

$$(3)(-3,6)$$

$$(4)(-3,1)$$

Sol. (3)

$$S_1 + \lambda(S_1 - S_2) = 0$$

$$x^2 + y^2 - 6x + \lambda(4y - 6x) = 0$$

$$x^2 + y^2 - 6x(1 + \lambda) + 4\lambda y = 0$$
Centre $(3(1 + \lambda), -2\lambda)$ put in $2x - 3y + 12 = 0$

$$6 + 6\lambda + 6\lambda + 12 = 0$$

$$12\lambda = -18$$

$$\lambda = -3/2$$

$$\therefore \text{ Circle is } x^2 + y^2 + 3x - 6y = 0$$
Check options

Q.21 Let $\{x\}$ and [x] denote the fractional part of x and the greatest integer $\le x$ respectively of a real number x. If $\int_0^n \{x\} dx$, $\int_0^n [x] dx$ and $10(n^2-n)$, $(n \in N, n > 1)$ are three consecutive terms of a G.P., then n is equal to_____

Sol. 21

$$\int_{0}^{n} \{x\} dx = n \int_{0}^{1} x dx = n \left(\frac{x^{2}}{2}\right) = \frac{n}{2}$$

$$\int_{0}^{n} [x] dx = \int_{0}^{1} 0 + \int_{1}^{2} 1 dx + \int_{2}^{3} 2 dx + \dots + \int_{n-1}^{n} (n-1) dx$$

$$= 1 + 2 + \dots + n - 1 \Rightarrow \frac{n(n-1)}{2}$$

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$$= \frac{n}{2}, \frac{n(n-1)}{2}, 10(n^2 - n) \rightarrow G.P$$

$$= \frac{n^2(n-1)^2}{4} = \frac{n}{2}.10.n(n-1)$$
n - 1 = 20; n = 21

- **Q.22** A test consists of 6 multiple choice questions, each having 4 alternative answers of which only one is correct. The number of ways, in which a candidate answers all six questions such that exactly four of the answers are correct, is ______
- **Sol.** 135 ${}^{6}C_{4} \times 1 \times 3^{2} = 15 \times 9 = 135$
- **Q.23** If $\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k}$, then the value of $\left|\hat{i} \times \left(\vec{a} \times \hat{i}\right)\right|^2 + \left|\hat{j} \times \left(\vec{a} \times \hat{j}\right)\right|^2 + \left|\hat{k} \times \left(\vec{a} \times \hat{k}\right)\right|^2$ is equal to_____
- Sol. 18

$$\left|\hat{i} \times \left(\vec{a} \times \hat{i}\right)\right|^2 = \left|\vec{a} - \left(a\hat{i}\right)\hat{i}\right|^2$$

$$= \left| \hat{j} + 2\hat{k} \right|^2 = 1 + 4 = 5$$

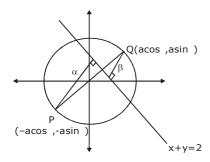
Similarly

$$\left|\hat{j} \times (\vec{a} \times \hat{j})\right|^2 = \left|2\hat{i} + 2\hat{k}\right|^2 = 4 + 4 = 8$$

$$\left|\hat{k} \times \left(\vec{a} \times \hat{k}\right)\right|^2 = \left|2\hat{i} + \hat{j}\right|^2 = 4 + 1 = 5$$

$$\Rightarrow 5 + 8 + 5 = 18$$

- Q.24 Let PQ be a diameter of the circle $x^2+y^2=9$. If α and β are the lengths of the perpendiculars from P and Q on the straight line, x+y=2 respectively, then the maximum value of $\alpha\beta$ is _____
- Sol. 7



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$$\alpha = \left| \frac{3\cos\theta + 3\sin\theta - 2}{\sqrt{2}} \right|$$

$$\beta = \left| \frac{+3\cos\theta + 3\sin\theta + 2}{\sqrt{2}} \right|$$

$$\alpha\beta = \left| \frac{\left(3\cos\theta + 3\sin\theta \right)^2 - 4}{2} \right| \Rightarrow \alpha\beta = \left| \frac{9 + 9\sin 2\theta - 4}{2} \right| \Rightarrow \alpha\beta = \left| \frac{5 + 9\sin 2\theta}{2} \right|$$

$$\alpha\beta_{\text{max}} = \frac{9+5}{2} = 7$$

Q.25 If the variance of the following frequency

distribution:

Sol.

$$6^2 = \frac{\sum f_i x_i^2}{\sum f_i} - \left(\frac{\sum f_i x_i}{\sum f_i}\right)^2$$

$$x_i$$
 f_i $x - \overline{x}$ $(x - \overline{x})^2$ $f_i(x - \overline{x})^2$

$$\overline{4+x}$$

$$\overline{x} = \frac{100 + 25x}{4 + x}$$

$$\overline{x} = 25$$

$$\therefore \frac{400}{4+x} = 50$$

$$x = 4$$

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